Philadelphia University Department of Basic Sciences and Mathematics

| Academic Year: | $2016-2017$ | Course Name: | Linear Programming |
| :--- | :--- | :--- | :--- |
| Semester: | Summer Semester | Course Number: | 250373 |
| Exam: | Second Exam | Instructor Name: | Feras Awad |
| Exam Date: | $08 / 08 / 2017$ | Student Name: | - |
| Exam Day: | Tuesday | University ID: | - |
| Exam Mark: | $[20]$ | Serial: | - |

1. (6 points) Use the Big M-method to solve the following problem.

$$
\begin{array}{rr}
\text { Maximize } & z=x_{1}+5 x_{2}+3 x_{3} \\
\text { Subject to } & x_{1}+2 x_{2}+x_{3}=3 \\
& 2 x_{1}-x_{2}=4 \\
& x_{1}, x_{2}, x_{3} \geq 0
\end{array}
$$



Time : 60 Minutes
2. (8 points) Find the optimal tableau using the laws of matrices for the following LP if $x_{2}$ and $s_{2}$ are the basic optimal solution set of the problem.

$$
\begin{aligned}
\text { Maximize } & z=2 x_{1}+5 x_{2} \\
\text { Subject to } & x_{1}+2 x_{2} \leq 16 \\
& x_{1}-x_{2} \leq 12 \\
& x_{1}, x_{2} \geq 0
\end{aligned}
$$

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$


Time : 60 Minutes
3. (6 points) Determine whether the following problem has

- unique optimal solution, or $\quad$ Maximize $z=2 x_{1}-x_{2}+3 x_{3}$
- alternative optimal solution(s), or
- unbounded solution.

| Maximize | $z=2 x_{1}-x_{2}+3 x_{3}$ |  |
| :---: | :---: | :---: |
| Subject to | $x_{1}-x_{2}+5 x_{3} \leq 10$ |  |
|  | $2 x_{1}-x_{2}+3 x_{3} \leq 40$ |  |
|  | $x_{1}, x_{2}, x_{3} \geq 0$ |  |


| $z$ |  | RHS |
| :---: | :--- | :--- |
| Row 0 |  |  |
|  |  |  |
| Row 0 |  |  |
|  |  |  |
| Row 0 |  |  |
|  |  |  |
| Row 0 |  |  |
| Row 0 |  |  |
|  |  |  |
| Row 0 |  |  |
|  |  |  |

