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Lect 6

"Intensity Transformation and spatial filtering"

Definition: Image enhancement is the process that improves the quality of the image for a specific application.

Image enhancement methods:

- spatial domain methods (image plane)

techniques are based on direct manipulation of pixels in an image.

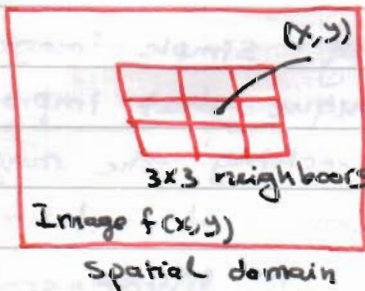
- Frequency domain methods:

Techniques are based on modifying the Fourier transform of the image.

- Combinations methods:

There are some enhancement techniques based on various combinations of methods from the two first categories.

origin



procedures that operate directly on pixels (spatial domain) can be denoted by the expression:

$$g(x, y) = T[f(x, y)].$$

where: $f(x, y)$ is the input image, $g(x, y)$ is the processed (output) image

T is an operator on $f(x, y)$ defined over some neighborhood of (x, y) .

Mask / filter: neighborhood of a point (x, y) can be used, by using a square/rectangular (common used) or circular sub image area centered at (x, y) .

The center of the subimage is moved from pixel to pixel starting at the top of the corner.

• point processing:

- Neighborhood: 1×1 pixel.

- g depends on only the value of f at (x, y) .

and T becomes an intensity transformation function (gray-level or mapping function) of the form :

$$S = T(r)$$

where : r = gray level of $f(x,y)$
 s = gray level of $g(x,y)$

T is a function that maps r to s

examples :

① Contrast stretching : (normalization)

if $T(r)$ has the form as shown in figure, the effect of applying the transformation to every pixel of f to generate the corresponding pixels in g would :

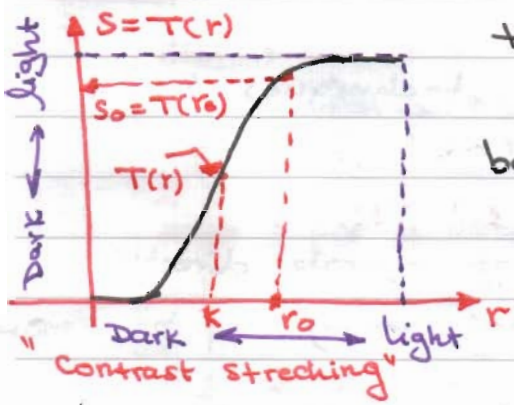
- produce higher contrast than the original by :

* darkening the levels

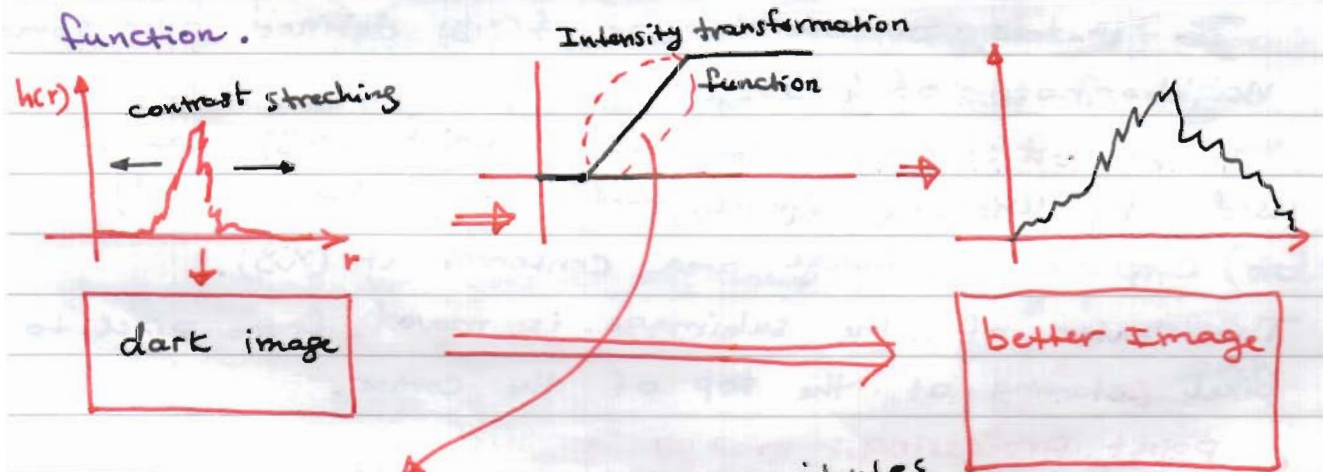
below k in the original image.

* brightening the levels

above k in the original image.

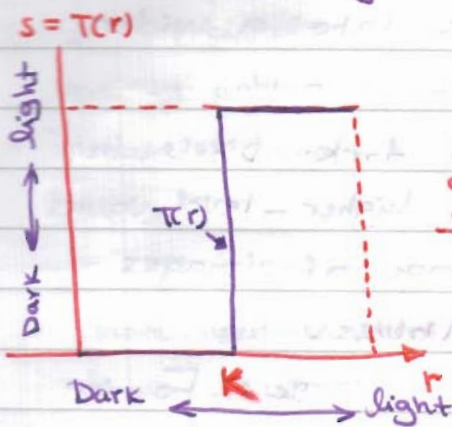


Contrast stretching : Simple image enhancement technique that improves the contrast in an image by 'stretching' the range of intensity values it contains to span a desired range of values. Typically, it uses a linear scaling function.



linear part contributes to the contrast stretching.

② Thresholding : Produce a two-level (binary)



Image, a mapping of this form called thresholding function.

Some Basic Intensity Transformation Functions

three basic types of functions used frequently for image enhancement :

1- linear functions : negative and Identity transformations.

2- Logarithmic : Log and Inverse Log transformations.

3- Power-Law functions (n^{th} power and n^{th} root transformations,

(as shown in figure) :

① Identity function :

- output intensities are identical to input intensities.

- Is included in the graph only

for completeness.

② Image negatives :

The negative of an image with gray level in the range $[0, L-1]$, where $L = 2^n$, $n = 1, 2, \dots$ is obtained by using the negative transformation's expression :

$$s = L - 1 - r$$

that reverses the intensity levels of an input image.

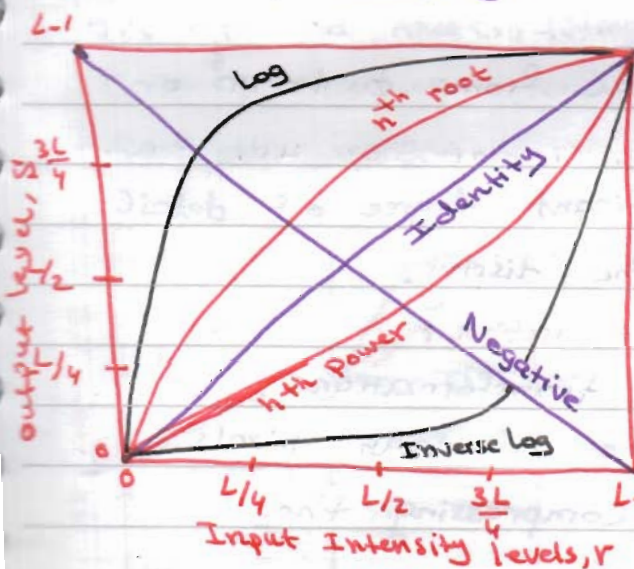
The negative transformation is suitable for enhancing white or gray detailed embedded in dark regions of an image, especially when the black area are dominant in size.

③ Log Transformation :

The general form of the log transformation :

$$S = C \cdot \log(1 + r)$$

C is a constant, and $r \geq 0$.



- Log Curve maps a narrow range of low gray-level values in the input image into a wider range of the output levels.
- Used to expand the values of dark pixels in an image while compressing the higher-level values.
- it compresses the dynamic range of images with large variations in pixel values.
- Example of image with dynamic range: Fourier spectrum image.
- it can have intensity range from 0 to 10^6 or higher.
- We can't see the significant degree of detail as it will be lost in the display.

④ Inverse Logarithm Transformation:

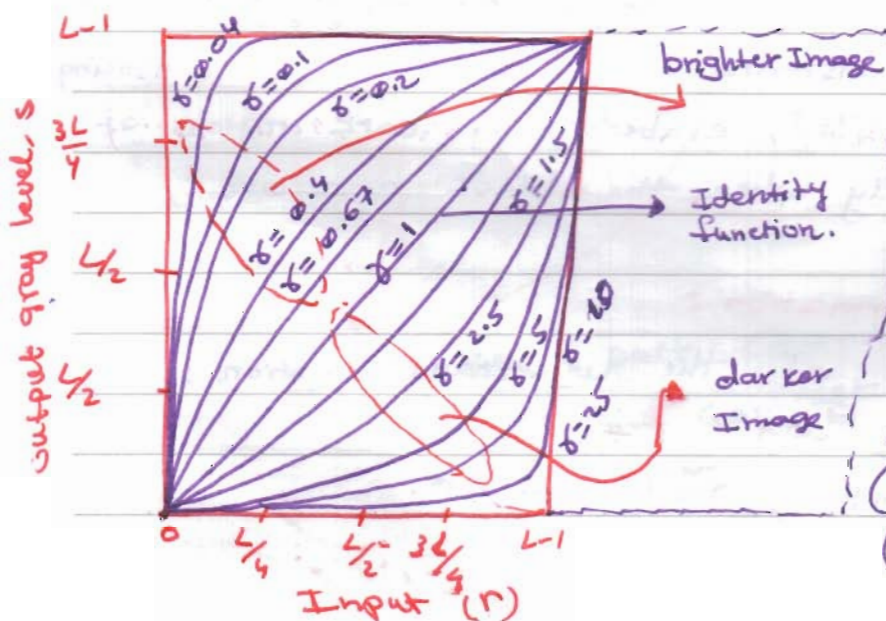
- Do opposite to the log transformations.
- Used to expand the values of high pixels in an image while compressing the darker-level values.

⑤ Power-Law (Gamma) Transformation:

The general form of the power-law transformation:

$$S = C \cdot r^\gamma, \text{ where } C \text{ and } \gamma \geq 0.$$

- different transformations curves are obtained by varying γ (gamma).



Many Image capturing, printing and display devices use gamma correction, which enhances the given images by power-law response phenomena.

for example:
CRT device
(Cathode Ray tube)
($\gamma = 1.8 - 2.5$)

Piecewise - linear Transformation Functions:

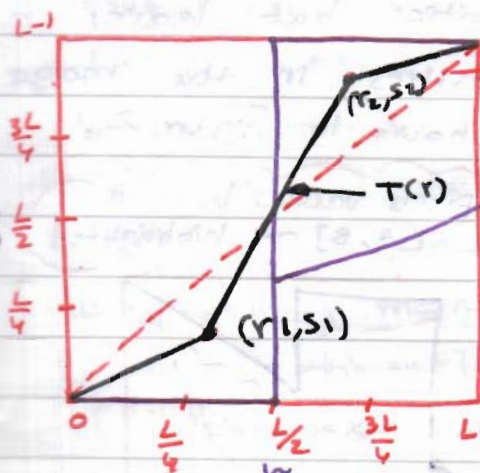
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- principal advantage: the form of piecewise function can be arbitrarily complex (more options to design), some important transformations can be formulated only as piecewise functions.

- The principal disadvantage: their specification requires more user input.

1) Contrast stretching:

one of the most (simplest) piecewise function is the Contrast stretching, which is used to enhance the low contrast images.



① $s_1 = r_1$ and $s_2 = r_2$ (Identity transformation)
(No changes in the image)

② $r_1 = r_2$, $s_1 = 0$, and $s_2 = L-1$
(thresholding function - Image converted to black & white).

③ Intermediate values of (r_1, s_1) and (r_2, s_2) produces various degree of

spread in the intensity levels of the output image, in general, $r_1 \leq r_2$ and $s_1 \leq s_2$, so the function is single valued and monotonically increasing.

example: to enhance an 8-bit image with low contrast using contrast stretching, and obtained by setting:

$$(r_1, s_1) = (r_{\min}, 0) \text{ and } (r_2, s_2) = (r_{\max}, L-1)$$

where r_{\min} & r_{\max} denote the minimum and the maximum intensity levels in the image \rightarrow so

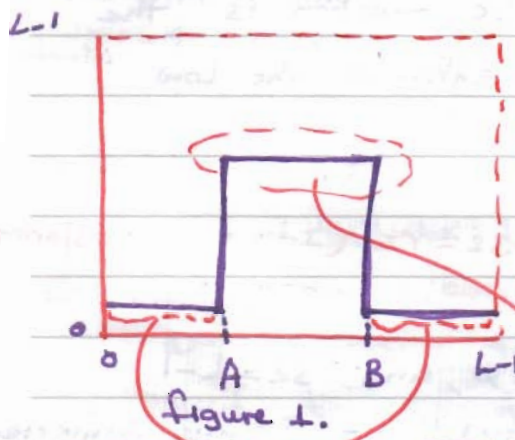
the transformation function stretches the levels

linearly from their original range to the full range $[0, L-1]$.

2) Gray-Level Slicing (Intensity-level slicing).

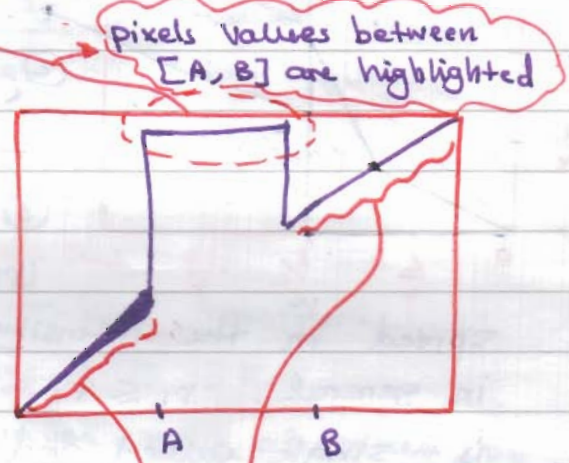
This technique is used to highlight a specific range of gray levels in a given image, The process, often called intensity-level slicing, and can be implemented in several way

a) Display all values in the range of interest in one value (say, white), and all other intensities in another value (say, black). as shown in figure 1., this transformation produces a binary image.



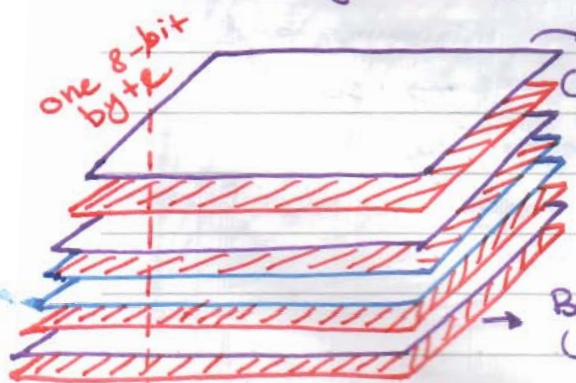
This transformation highlights range [A, B] of gray levels and reduces all others to a contrast level, other pixels are darkened.

b) The second approach. brightens (or darkens) the desired range of intensities but leaves all other intensities in the image unchanged, as shown in figure 2.



3) Bit-plane slicing :

pixels are digital number composed of bits, Instead of highlighting intensity-level range, We could highlighting the contribution made by each bit,



this method is useful and used in image compression.

Figure: Bit-plane representation of an 8-bit image

most significant bits contains the majority of the visually significant data