



*Philadelphia University*  
*Faculty of Engineering*

**Marking Scheme**

Exam Paper

BSc CE

**Neural Networks and Fuzzy Logic (630514)**

Second Exam

Summer semester

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Section 1

Weighting 20% of the module total

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**Question 2** This question is attributed with 4 marks if answered properly; the answers are as following:

**Solution**

**Step 1: Initialization**

Set initial weights  $w_1, w_2, \dots, w_n$  and threshold  $\theta$  to random numbers in the range  $[-0.5, 0.5]$ .

**Step 2: Activation**

Activate the perceptron by applying inputs  $x_1(p), x_2(p), \dots, x_n(p)$  and desired output  $Y_d(p)$ . Calculate the actual output at iteration  $p = 1$

$$Y(p) = \text{step} \left[ \sum_{i=1}^n x_i(p) w_i(p) - \theta \right]$$

Where  $n$  is the number of the perceptron inputs, and **step** is a step activation function.

**Step 3: Weight training**

Update the weights of the perceptron

$$w_i(p+1) = w_i(p) + \Delta w_i(p)$$

where  $\Delta w_i(p)$  is the weight correction at iteration  $p$ .

$$\Delta w_i(p) = \alpha \cdot x_i(p) \cdot e(p)$$

The weight correction is computed by the delta rule:

**Step 4: Iteration**

Increase iteration  $p$  by one, go back to **Step 2** and repeat the process until convergence.

**Question 3** This question is attributed with 5 marks if answered properly; the answers are as following:

**Solution**

**a) Forward Pass**

Input to top neuron =  $(0.1 \times 0.1) + (0.7 \times 0.5) = 0.36$ . Out = **0.589**.

Input to bottom neuron =  $(0.1 \times 0.3) + (0.7 \times 0.2) = 0.17$ . Out = **0.5424**.

Input to final neuron =  $(0.589 \times 0.2) + (0.5424 \times 0.1) = 0.17204$ . Out = **0.5429**.

**b) Reverse Pass**

Output error  $\delta = (t-o)(1-o)o = (1-0.5429)(1-0.5429)0.5429 = \mathbf{0.11343}$ .

New weights for output layer

$w1(+)$  =  $w1 + (\delta \times \text{input}) = 0.2 + (0.11343 \times 0.589) = \mathbf{0.2668}$ .

$w2(+)$  =  $w2 + (\delta \times \text{input}) = 0.1 + (0.11343 \times 0.5424) = \mathbf{0.16152}$ .

Errors for hidden layers:

$\delta 1 = \delta \times w1 = 0.11343 \times 0.2668 = 0.030263(x(1-o)o) = \mathbf{0.007326}$ .

$\delta 2 = \delta \times w2 = 0.11343 \times 0.16152 = 0.018321(x(1-o)o) = \mathbf{0.004547}$ .

New hidden layer weights:

$w3(+)$  =  $0.1 + (0.007326 \times 0.1) = \mathbf{0.1007326}$ .

$w4(+)$  =  $0.5 + (0.007326 \times 0.7) = \mathbf{0.505128}$ .

$w5(+)$  =  $0.3 + (0.004547 \times 0.1) = \mathbf{0.3004547}$ .

$w6(+)$  =  $0.2 + (0.004547 \times 0.7) = \mathbf{0.20318}$ .

**Question 4** This question is attributed with 3 marks if answered properly; the answers are as following:

**(a) AND ( $x_1, x_2$ ) Solution**

$$W = x_1 x_1^T + x_2 x_2^T = \begin{bmatrix} 1 \\ -1 \\ -1 \\ 1 \end{bmatrix} \begin{bmatrix} 1 & -1 & -1 & 1 \end{bmatrix} + \begin{bmatrix} -1 \\ 1 \\ 1 \\ -1 \end{bmatrix} \begin{bmatrix} -1 & 1 & 1 & -1 \end{bmatrix}$$

$$W = \begin{bmatrix} 1 & -1 & -1 & 1 \\ -1 & 1 & 1 & -1 \\ -1 & 1 & 1 & -1 \\ 1 & -1 & -1 & 1 \end{bmatrix} + \begin{bmatrix} 1 & -1 & -1 & 1 \\ -1 & 1 & 1 & -1 \\ -1 & 1 & 1 & -1 \\ 1 & -1 & -1 & 1 \end{bmatrix} = \begin{bmatrix} 2 & -2 & -2 & 2 \\ -2 & 2 & 2 & -2 \\ -2 & 2 & 2 & -2 \\ 2 & -2 & -2 & 2 \end{bmatrix}$$

Since we demand that all  $w_{ii} = 0$ , we get:

$$W = \begin{bmatrix} 0 & -2 & -2 & 2 \\ -2 & 0 & 2 & -2 \\ -2 & 2 & 0 & -2 \\ 2 & -2 & -2 & 0 \end{bmatrix}$$