

# Internal combustion engines



## Chapter two

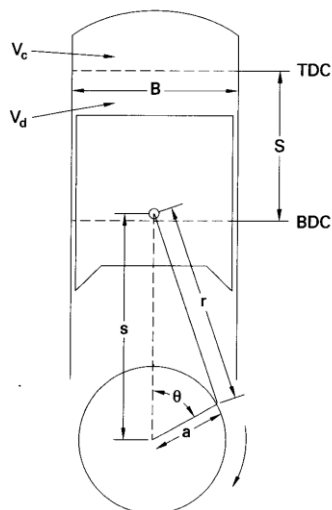
### OPERATION IC ENGINES

#### Section 2.1 ENGINE PARAMETERS

By

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### OPERATION IC ENGINES



$$\square S = 2a$$

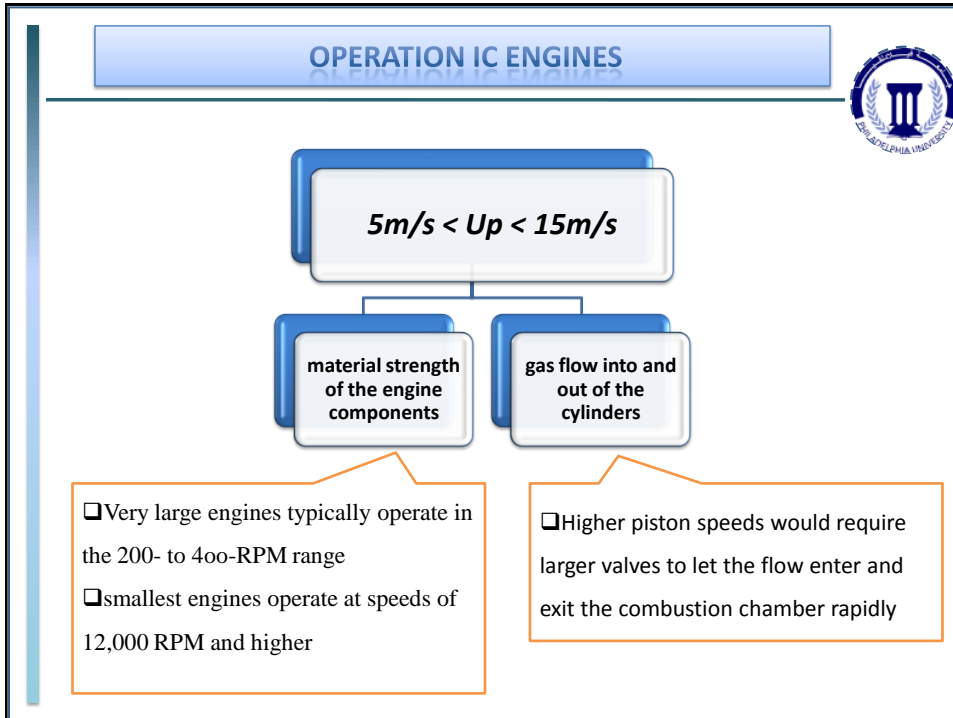
$\square$  Average piston speed is:

$$\overline{U}_p = 2(S)(N)$$


$\square N$  is generally given in RPM

$$\square 5m/s < U_p < 15m/s$$

**Figure 2-1** Piston and cylinder geometry of reciprocating engine.  $B$  = bore;  $S$  = stroke;  $r$  = connecting rod length;  $a$  = crank offset;  $s$  = piston position;  $\theta$  = crank angle;  $V_c$  = clearance volume;  $V_d$  = displacement volume.

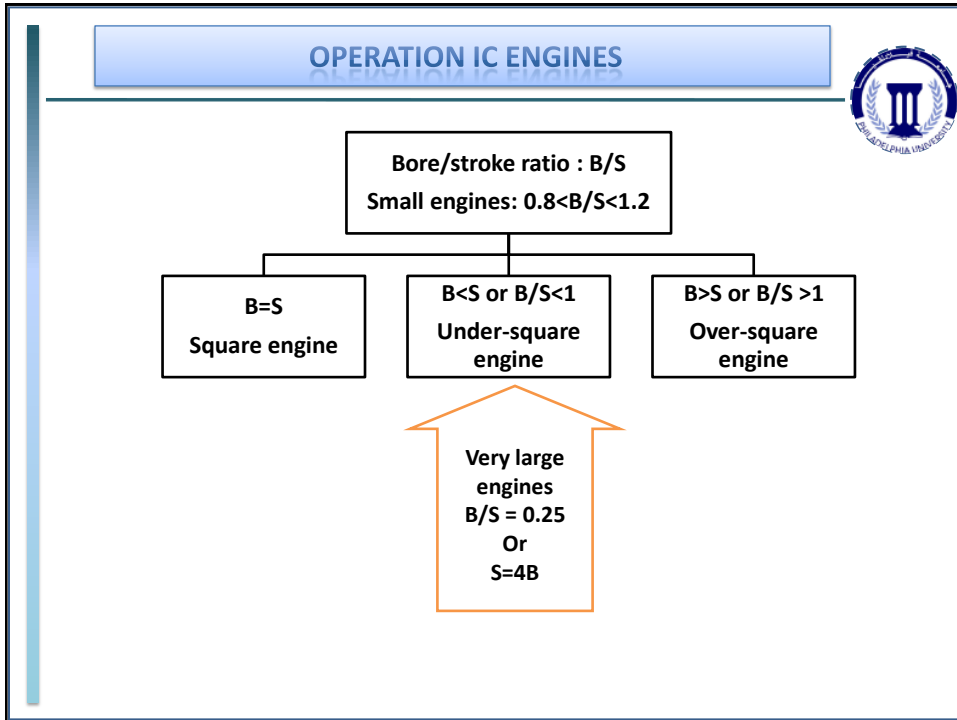


## OPERATION IC ENGINES



**TABLE 2-1 TYPICAL ENGINE OPERATING PARAMETERS**

	Model Airplane Two-Stroke Cycle	Automobile Four-Stroke Cycle	Large Stationary Two-Stroke Cycle
BORE (cm)	2.00	9.42	50.0
STROKE (cm)	2.04	9.89	161
DISPLACEMENT/cyl (L)	0.0066	0.69	316
SPEED (RPM)	13,000	5200	125
POWER/cyl (kW)	0.72	35	311
AVERAGE PISTON SPEED (m/sec)	8.84	17.1	6.71
POWER/DISPLACEMENT (kW/L)	109	50.7	0.98
bmp (kPa)	503	1170	472



**OPERATION IC ENGINES**

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$$s = a \cos(\theta) + \sqrt{r^2 - a^2 \sin^2(\theta)}$$

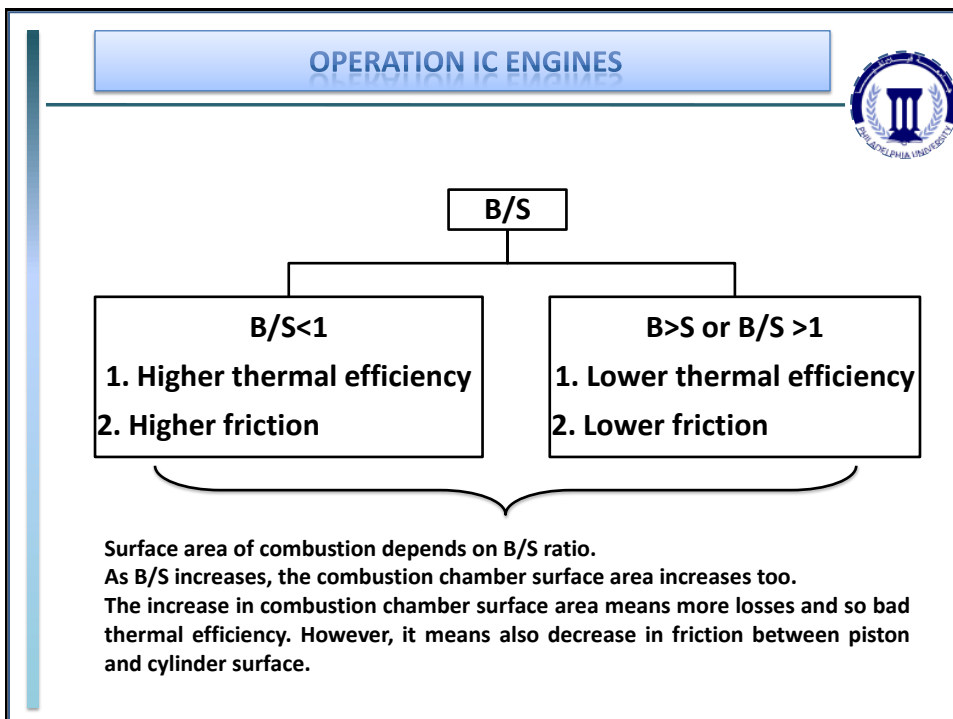
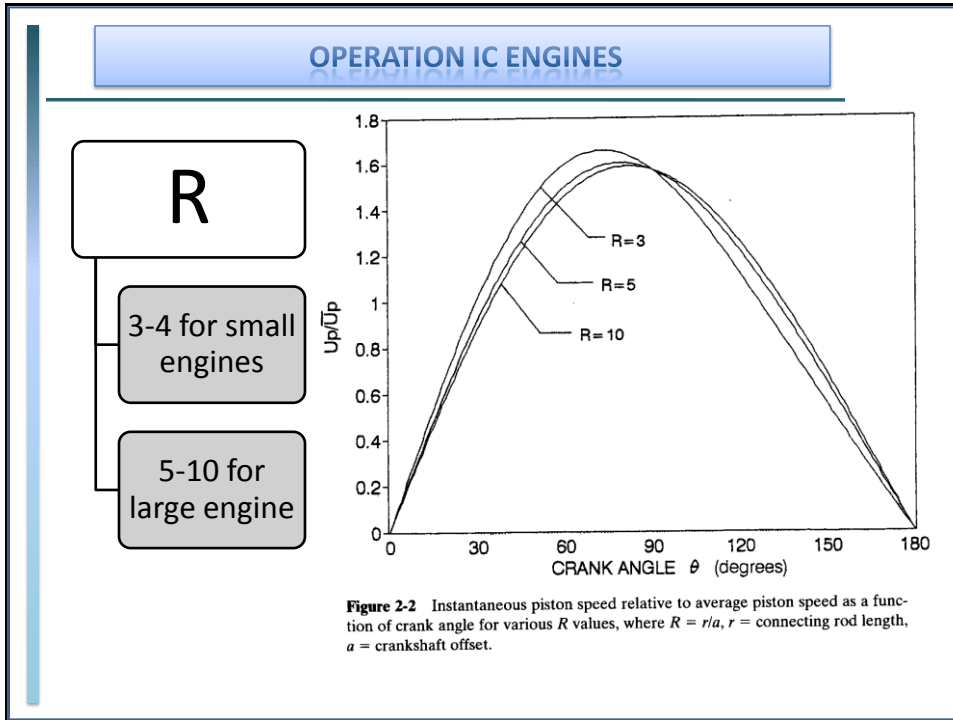
**Where:**

- a: crank offset
- r: connecting rod length
- $\theta$ : crank angle

**The instantaneous piston speed  $U_p$ :**

$$U_p = ds/dt$$

$$\frac{U_p}{U_p} = \frac{\pi}{2} \sin(\theta) \left[ \frac{\cos(\theta)}{\sqrt{R^2 - \sin^2(\theta)}} \right]; R = \frac{r}{a}$$



## OPERATION IC ENGINES



**Displacement volume ( $V_d$ ):**  $V_d = V_{BDC} - V_{TDC}$

And so:  $V_d = \left(\frac{\pi}{4}\right) B^2 S$

For engine with  $N_c$  cylinders:  $V_d = N_c \left(\frac{\pi}{4}\right) B^2 S$

**Clearance volume ( $V_c$ ):**  $V_c = V_{TDC} \rightarrow V_{BDC} = V_c + V_d$

**Compression ratio ( $r_c$ ):**  $r_c = \frac{V_{BDC}}{V_{TDC}} = \frac{V_c + V_d}{V_c}$

## OPERATION IC ENGINES

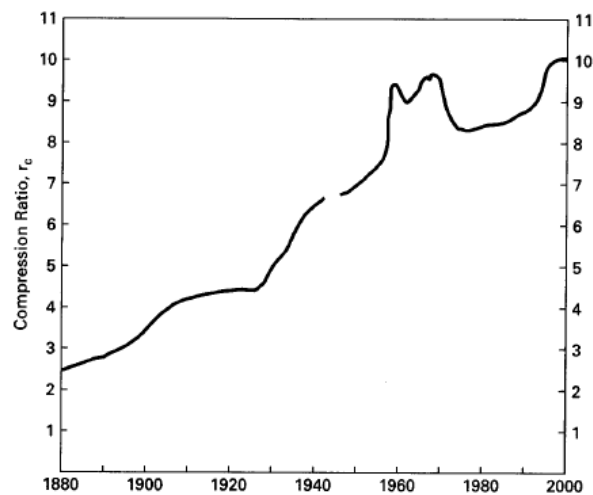


always  $r_c > 1$

spark ignition (SI):  
8 to 11

compression  
ignition (CI):  
12 to 24

Adding charger  
reduce  $r_c$ .



## OPERATION IC ENGINES



The cylinder volume  $V$  at any crank angle is:

$$V = V_c + (\pi B^2/4)(r + a - s) \quad (2-13)$$

where:  $V_c$  = clearance volume

$B$  = bore

$r$  = connecting rod length

$a$  = crank offset

$s$  = piston position shown in Fig. 2-1

This can also be written in a non-dimensional form by dividing by  $V_c$ , substituting for  $r$ ,  $a$ , and  $s$ , and employing the definition of  $R$ :

$$V/V_c = 1 + \frac{1}{2}(r_c - 1)[R + 1 - \cos\theta - \sqrt{R^2 - \sin^2\theta}] \quad (2-14)$$

where:  $r_c$  = compression ratio

$R = r/a$

## OPERATION IC ENGINES



The cross-sectional area of a cylinder and the surface area of a flat-topped piston are each given by:

$$A_p = (\pi/4)B^2 \quad (2-15)$$

The combustion chamber surface area is:

$$A = A_{ch} + A_p + \pi B(r + a - s) \quad (2-16)$$

where  $A_{ch}$  is the cylinder head surface area, which will be somewhat larger than  $A_p$ .

Then if the definitions for  $r$ ,  $a$ ,  $s$ , and  $R$  are used, Eq. (2-16) can be rewritten as:

$$A = A_{ch} + A_p + (\pi BS/2)[R + 1 - \cos\theta - \sqrt{R^2 - \sin^2\theta}] \quad (2-17)$$

## OPERATION IC ENGINES



### EXAMPLE PROBLEM 2-1

John's automobile has a three-liter SI V6 engine that operates on a four-stroke cycle at 3600 RPM. The compression ratio is 9.5, the length of connecting rods is 16.6 cm, and the engine is square ( $B = S$ ). At this speed, combustion ends at  $20^\circ$  aTDC.

Calculate:

1. cylinder bore and stroke length
2. average piston speed
3. clearance volume of one cylinder
4. piston speed at the end of combustion
5. distance the piston has traveled from TDC at the end of combustion
6. volume in the combustion chamber at the end of combustion

## OPERATION IC ENGINES



- 1) For one cylinder,

$$V_d = V_{\text{total}}/6 = 3\text{L}/6 = 0.5\text{ L} = 0.0005\text{ m}^3 = (\pi/4)B^2S = (\pi/4)B^3$$

$$\underline{B = 0.0860\text{ m} = 8.60\text{ cm} = S}$$

2)  $\bar{U}_p = 2SN = (2\text{ strokes/rev})(0.0860\text{ m/stroke})(3600/60\text{ rev/sec})$   
 $\underline{= 10.32\text{ m/sec}}$

3)  $r_c = 9.5 = (V_d + V_c)/V_c = (0.0005 + V_c)/V_c$   
 $\underline{V_c = 0.000059\text{ m}^3 = 59\text{ cm}^3}$

- 4) Crank offset,  $a = S/2 = 0.0430\text{ m} = 4.30\text{ cm}$

$$R = r/a = 16.6\text{ cm}/4.30\text{ cm} = 3.86$$

$$\begin{aligned} U_p/\bar{U}_p &= (\pi/2) \sin \theta [1 + (\cos \theta / \sqrt{R^2 - \sin^2 \theta})] \\ &= (\pi/2) \sin (20^\circ) \{1 + [\cos (20^\circ) / \sqrt{(3.86)^2 - \sin^2 (20^\circ)}]\} \\ &= 0.668 \end{aligned}$$

$$\underline{U_p = 0.668 \bar{U}_p = (0.668)(10.32\text{ m/sec}) = 6.89\text{ m/sec}}$$

## OPERATION IC ENGINES



$$\begin{aligned}
 5) \quad s &= a \cos \theta + \sqrt{r^2 - a^2 \sin^2 \theta} \\
 &= (0.0430 \text{ m}) \cos(20^\circ) + \sqrt{(0.166 \text{ m})^2 - (0.0430 \text{ m})^2 \sin^2(20^\circ)} \\
 &= 0.206 \text{ m}
 \end{aligned}$$

Distance from TDC:

$$\begin{aligned}
 x &= r + a - s = (0.166 \text{ m}) + (0.043 \text{ m}) - (0.206 \text{ m}) \\
 &= \underline{0.003 \text{ m} = 0.3 \text{ cm}}
 \end{aligned}$$

$$\begin{aligned}
 6) \quad V/V_c &= 1 + \frac{1}{2}(r_c - 1)[R + 1 - \cos \theta - \sqrt{R^2 - \sin^2 \theta}] \\
 &= 1 + \frac{1}{2}(9.5 - 1)[3.86 + 1 - \cos(20^\circ) - \sqrt{(3.86)^2 - \sin^2(20^\circ)}] \\
 &= 1.32
 \end{aligned}$$

$$V = 1.32 V_c = (1.32)(59 \text{ cm}^3) = \underline{77.9 \text{ cm}^3 = 0.0000779 \text{ m}^3}$$