

Question 2:**(4 Marks)****Objectives:** This question is about Newton-Raphson Iterative Method.

Given the following non-linear equation, it is required to solve it using N-R iterative method. Start with $x_0 = 0.4$ and approximate the root with a relative error $\leq 5\%$.

$$f(x) = 8\sin(x)e^{-x} - 1$$

Question 3:**(6 Marks)****Objectives:** This question is about Gauss-Sidel iterative method.

Given the following system of linear equations, it is required to apply 3-iteration using Gauss-Sidel iterative method and find the absolute error in the last iteration.

$$\begin{aligned} 5x - 2y + z &= 11 \\ -2x + 6y - 3z &= -7 \\ x + 2y + 4z &= 36 \end{aligned}$$

Question 4:**(6 Marks)****Objectives:** This question is about interpolation.

Estimate $f(1)$ for the following readings by using 3rd order Newton interpolating polynomial.

x	1.2	1.4	1.6	1.8
f(x)	5.72	5.28	4.68	3.92

Question 5:**(6 Marks)****Objectives:** This question is about numerical integration.

Use 7-sample point of 1/3 composite Simpson's rule to approximate the integral of the following function over the interval $x=1$ to $x=10$.

$$f(x) = x^2 \log(x + \sqrt{x^2 + 1})$$

Question 6:**(6 Marks)****Objectives:** This question is about 2nd order Runge-Kutta (Huen's) numerical integration method.

Given $\frac{dy}{dx} = \frac{\cos(6x)}{(y^2 + x + 1)}$ with $y(0)=0.1$, it is required to find $y(0.2)$ using Huen's

numerical integration method with step size $h=0.1$.

Good Luck