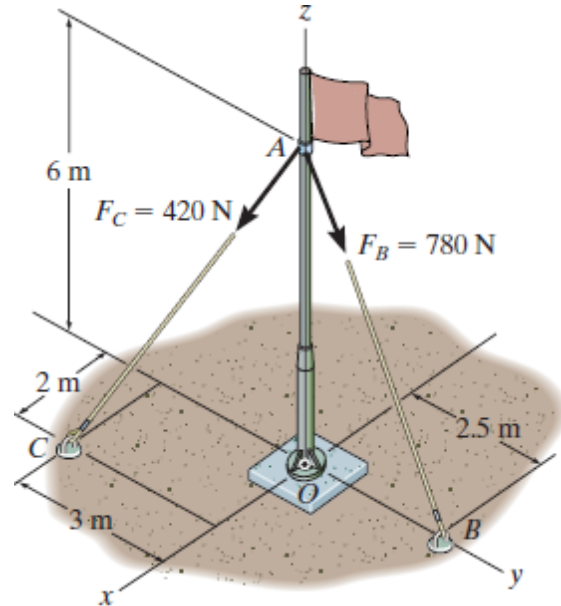


Determine the moment produced by force F_B about point O .



$$\mathbf{r}_{OA} = [6\mathbf{k}] \text{ m}$$

$$\mathbf{r}_{OB} = [2.5\mathbf{j}] \text{ m}$$

The force vector \mathbf{F}_B is given by

$$\mathbf{F}_B = F_B \mathbf{u}_{FB} = 780 \frac{(0-0)\mathbf{i} + (2.5-0)\mathbf{j} + (0-6)\mathbf{k}}{\sqrt{(0-0)^2 + (2.5-0)^2 + (0-6)^2}} = [300\mathbf{j} - 720\mathbf{k}] \text{ N}$$

Vector Cross Product: The moment of \mathbf{F}_B about point O is given by

$$\mathbf{M}_O = \mathbf{r}_{OA} \times \mathbf{F}_B = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 0 & 0 & 6 \\ 0 & 300 & -720 \end{vmatrix} = [-1800\mathbf{i}] \text{ N} \cdot \text{m} = [-1.80\mathbf{i}] \text{ kN} \cdot \text{m}$$

or

$$\mathbf{M}_O = \mathbf{r}_{OB} \times \mathbf{F}_B = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 0 & 2.5 & 0 \\ 0 & 300 & -720 \end{vmatrix} = [-1800\mathbf{i}] \text{ N} \cdot \text{m} = [-1.80\mathbf{i}] \text{ kN} \cdot \text{m}$$

•2-33. If $F_1 = 600\text{ N}$ and $\phi = 30^\circ$, determine the magnitude of the resultant force acting on the eyebolt and its direction measured clockwise from the positive x axis.

Rectangular Components: By referring to Fig. *a*, the x and y components of each force can be written as

$$\begin{aligned} (F_1)_x &= 600 \cos 30^\circ = 519.62\text{ N} & (F_1)_y &= 600 \sin 30^\circ = 300\text{ N} \\ (F_2)_x &= 500 \cos 60^\circ = 250\text{ N} & (F_2)_y &= 500 \sin 60^\circ = 433.0\text{ N} \\ (F_3)_x &= 450 \left(\frac{3}{5}\right) = 270\text{ N} & (F_3)_y &= 450 \left(\frac{4}{5}\right) = 360\text{ N} \end{aligned}$$

Resultant Force: Summing the force components algebraically along the x and y axes,

$$\begin{aligned} +\rightarrow \Sigma (F_R)_x &= \Sigma F_x; & (F_R)_x &= 519.62 + 250 - 270 = 499.62\text{ N} \rightarrow \\ +\uparrow \Sigma (F_R)_y &= \Sigma F_y; & (F_R)_y &= 300 - 433.01 - 360 = -493.01\text{ N} \downarrow \end{aligned}$$

The magnitude of the resultant force F_R is

$$F_R = \sqrt{(F_R)_x^2 + (F_R)_y^2} = \sqrt{499.62^2 + 493.01^2} = 701.91\text{ N} \approx 702\text{ N}$$

Ans.

The direction angle θ of F_R , Fig. *b*, measured clockwise from the x axis, is

$$\theta = \tan^{-1} \left(\frac{(F_R)_y}{(F_R)_x} \right) = \tan^{-1} \left(\frac{493.01}{499.62} \right) = 44.6^\circ$$

